Validation of a Parabolic Equation method against long range blast wave measurements

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(U) Summary

This report is about the validation of a method, based on a Parabolic Equation model, for predicting acoustic noise. The method is designed for the low-frequency, long-ranging noise induced by heavy weapons and explosions. It is able to take detailed meteorological information into account, which is important for this application. Hundreds of relevant blast wave measurements are available from the Norwegian Trials campaign at Finnskogen. Fairly detailed weather data are also available from the campaign. We have compared our simulations with measurements from Finnskogen, and made the following main conclusions:

1. The PE model worked as well as can be expected given the parametric uncertainties.
2. Taking the weather into account is clearly necessary in noise mapping of heavy weapons.
3. The weather data improved the prediction accuracy of the PE model.
4. Prediction accuracy varied with weather type, season, distance and sound frequency.

A total of 299 unique combinations of detonation events and propagation paths have been considered, some of which were simulated several times with different parameter settings. The selected events were from six summer days and three winter days. Propagation distances varied from 1 to 23 km. Wind and temperature profiles were obtained from measurements that used a tethered balloon. Temperature inversions, which strongly influence sound propagation, occurred during both the summer and winter experiments. In the process of selecting and analysing the shot recordings and weather data, we found that there were errors and issues in the database registration, which are specified in this report. Future users of the database should therefore especially consult our chapters on shot selection and weather data.
(U) Sammendrag

Denne rapporten omhandler validering av en metode, basert på en Parabolic Equation-modell, for prediksjon av akustisk støy. Metoden er designet for lavfrekvent langtrekkende støy generert av tunge våpen og eksplosjoner. Den kan utnytte detaljert meteorologisk informasjon, noe som er sentralt for denne anvendelsen. Hundrevis av relevante lydmålinger er tilgjengelige fra Norwegian Trials-kampanjen på Finnskogen. Relativt detaljerte værdata er også tilgjengelige fra kampanjen. Vi har sammenliknet våre simuleringer med målinger fra Finnskogen, og kommet til følgende hovedkonklusjoner:

1. PE-modellen fungerte så bra som en kan forvente gitt parameterusikkerhetene.
2. Å ta hensyn til været er klart nødvendig for støykartlegging av tunge våpen.
3. Værdataene forbedret nøyaktigheten til PE-modellen.
4. Prediksjonenøyaktigheten varierte med værtype, årstid, avstand og lydfrekvens.

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1 Introduction

Military training activity produces acoustic noise that can affect neighbours, necessitating the ability to predict the noise dispersal. The software Milnoise serves as prediction tool for the Norwegian Defence. Predominantly, outdoors acoustics is concerned with traffic and industrial noise. Heavy weapons noise differs by being louder, lower in sound frequency and intermittent. In addition, the propagation is nonlinear near the source. With this particular application in mind, we have implemented a sound propagation model as presented in [18]-[19]. The purpose of this report is to validate the model, and our implementation, against measurements.

By far the most suitable data set available is from the Norwegian Trials at Finnskogen in the 1990s. The sound sources used, C4 charges from 1-64 kg, resemble the military sources; the terrain was predominantly Norwegian forest; the propagation distances were from 1-20 km. Weather data were gathered with a tethered sonde up to a few hundred meters above ground level, and there are data on the acoustic properties of the ground. The topography at the site is moderate, by Norwegian standards, ranging 280-450 m above sea level with few steep features.

A schematic overview of our propagation model, a parabolic equation (PE) model, is shown in Figure 1.1. Four categories of input data are indicated: source, weather, topography and ground impedance. The output data are sound levels. The weather data are of particular interest, as our main aim is to enable more detailed representation of refraction in the atmosphere.

The PE model is a rather established tool in outdoor acoustics, but most studies concern higher frequencies and shorter distances. We expect the model to capture the refractive effects accurately given precise weather data. Small scale turbulence effects may very well cause some difficulty, though. The treatment of the ground and the near-source nonlinearities are actually less well understood phenomena, however the resulting uncertainties may in practice be dominated by the strong impact of atmospheric refraction.

Since the main objective is to validate the PE model, use as detailed weather data as possible. In practice, meteorological data will always be a limiting element. Therefore, rather than as a validation of the propagation model, an alternative interpretation of this work is as a study of the predictive usefulness of the tethersonde data.

The report is organised in the following way: First, the Norwegian Trials data are introduced, and we describe how recordings were selected. The weather and ground data are then discussed, and interpreted as input data for the PE model. There is also a short section on source data. The simulations for summer conditions are presented first. Sections 3.1-3.2 discuss the simulations of 81 well documented cases from summer conditions. Those are perhaps the most important sections of this report. The remainder of that chapter presents simulations that further illuminate the findings. The winter simulations are presented in a similarly organised, separate chapter. Detailed plots of simulations and measurements can be found in the Appendix. The remainder of this introduction serves to introduce the propagation model, as well as some technical definitions.
Figure 1.1 Overview of the model. The sound pressure is given by $p = \Psi e^{-ikr}/\sqrt{r}$. Colours indicate relative sound levels for a 20 Hz harmonic source. The shown boundary condition is a bit simplified.

1.1 Basic notions and definitions

Cylindrical symmetry around the source location is assumed in the model, hence the sound pressure $p$ is considered a function of time $t$, the horizontal distance $r$, referred to as range, and height above ground $z$.

Fourier transforming in time, we get the complex pressure $p_f(r, z)$ for each frequency $f$. The sound pressure level is defined as

$$L_p(f) = 10 \log_{10} \left| \frac{p_f}{p_{\text{ref}}} \right|^2, \quad p_{\text{ref}} = 2 \times 10^{-5} \text{ Pa}. \quad (1.1)$$

For a point source it can be decomposed as

$$L_p(f) = L_0(f) - 10 \log_{10} \left( \frac{R}{R_0} \right)^2 + \Delta L_f, \quad (1.2)$$

where $L_0$ is the sound pressure level in a homogeneous free atmosphere at some reference distance $R_0$, the second term is the geometric loss, and $\Delta L_f$ is called the relative sound level. Hence, $\Delta L_f$ contains all information about refraction, terrain and ground effects and is independent of the source. Equation (1.2) is only valid for linear sound propagation out from a point source. Linearity may not hold near the source, but the nonlinear effects are, as an approximation, incorporated in the source data $L_0$. More details on source data can be found in [6].

The sound exposure level (SEL) is defined by

$$\text{SEL} = 10 \log_{10} \int_{t_{\text{ref}}} t_{\text{ref}}^{-1} \left| \frac{p}{p_{\text{ref}}} \right|^2 dt = 10 \log_{10} t_{\text{ref}}^{-1} \int \left| \frac{p_f}{p_{\text{ref}}} \right|^2 df, \quad (1.3)$$
with the reference time \( t_{\text{ref}} = 1 \) s and \( p_{\text{ref}} = 2 \times 10^{-5} \) Pa. All the calculations are performed in the frequency domain. Frequencies are sampled over 12th octaves, i.e. \( f_j = 2^{j/12} f_0 \) for integer \( j \). The sound exposure level in third octave bands \( \text{SEL}_3(f_c) \) for a center frequency \( f_c \) are reported. We use a standard trapezoidal rule to compute \( \text{SEL}_3 \) from twelfth octave samples.

The third octave bands from 1-100 Hz are considered here. Some of these are inaudible, hence it is common to 'C-weigh' the data, meaning that a standardised high pass filter cutting off at 20 Hz is applied. We denote the C-weighted SEL by \( \text{SEL}_{C} \).

Sound gets refracted in the atmosphere due to variations in the sound speed \( c \). We compute \( c \) from air temperature \( T \) according to the relation

\[
c = 340 \frac{m}{s} \sqrt{\frac{T}{288.15 K}}. \tag{1.4}
\]

The horizontal wind speed component \( u \) in the direction of propagation defines the effective sound speed \( c_{\text{eff}} = c + u \). We use the so-called effective sound speed approximation, which consists of an unmoving atmosphere with \( c \) replaced by \( c_{\text{eff}} \). By wave number \( k \) we therefore refer to the effective wave number \( \frac{2\pi f}{c_{\text{eff}}} \), strictly speaking.

The sound waves will interact with the ground, which is modeled as an impedance surface, meaning that the normal derivative of the complex pressure satisfies

\[
\frac{\partial p_f}{\partial n} = -\frac{ik}{Z} p_f \tag{1.5}
\]

at the ground surface, with the complex specific impedance \( Z \) depending strongly on frequency.

### 1.2 The PE method

The details of the PE method are described in [18]-[19]. We use the wide-angle PE equation of [11] (see [12]), with the exception that piecewise linear topographic profiles, rather than twice differentiable profiles are considered. The main equations are included in Figure [1.1]. Some numerical parameter choices for this study must be specified: The top of the domain was 15% of range, but never less than 250 m. We used 'reduction of range-dependence' as in [19] with an accuracy threshold of 5 m. As a 'scattering threshold' we generally used -35 dB, meaning that we did not allow the relative sound level \( \Delta L \) to drop below -35 dB.
2 Norwegian Trials data from Finnskogen

The campaigns at Finnskogen took place in September 1994 and February 1996. The geometry of the experiment is shown in Figure 2.1. C4 explosive was detonated at 2 m height on the locations marked in red. Towers with microphones were situated at five locations (yellow), and there were five weather towers with up to 30 m height (green). The tethersonde was operated at position 403. There are additional tethersonde data from positions 0 and 112, but we have not used them since they had more limited coverage. The weather measurements are summarised in [4]. We have accessed the Finnskogen data from the NORTRIAL database, described in [1] and [2], using the well-documented Matlab interface that comes along with it.

2.1 Shot selection

The recordings that we selected are listed in appendix A.4 and in this section the selection procedure is described. Each shot recording in the database has been assigned a quality label in the Nortrial database. Quality A recordings have a good signal-to-noise ratio and no other obvious issues. Quality B1 recordings are considered reliable except that the signal-to-noise ratio may be an issue. Other categories have not been considered here. In addition to quality labels, we have restricted ourselves to the times when the tethersonde was operated. Histograms of propagation distances are shown in Figure 2.2. We expect the farthest to be very challenging.

From summer 1994, we found 81 quality A cases that could be used. They are mostly from microphone towers 306 and 112. By a ‘case’ we mean a combination of a detonation event and a receiver position. For many cases there is more than one recording from a tower. If so, we picked the most elevated microphone. We have enumerated the cases according to the order they appear in the database listing, which seems to be chronological for summer data, and by tower, then chronological, for winter data.

The data from tower 0 appear not to be correctly registered, hence they were excluded. It appears as if the sampling rate cited is off by about a factor of two, although there could be other issues. This may have affected previous investigations of these data, and our advice is to ignore results using tower 0. We have performed the simulations however, in case the correct data were to be retrieved. This would add 46 quality A cases to the other 81.

From the winter trials, we have picked quality A data from February 21-23rd. We mostly consider data from tower 306, of which there are 83 cases. There are 73 quality A cases from 212 and 412, however it is clear that the charge sizes have been incorrectly registered there. By comparing to recordings of the same detonation events at 306, we have corrected the charges. This is also an issue for the summer data, but there was only one mismatch (case 122) and two that could not be verified (cases 40, 88), and it appears that we have gotten the charge sizes right.

A total of 61 quality B1 data from summer 1994 have briefly been considered. Since we had limited time to verify the quality, only those with SELC>70 dB were picked, of which six cases were excluded after inspection. Charge sizes were incorrect for many of these cases, and we excluded those were data entries disagreed.
Figure 2.1  Positioning of shots and measuring stations. Green dots are weather masts, yellow dots are sound recorder locations, red are shot positions. Tethersonde data are from 403. From [1].
Figure 2.2  Histograms of propagation distances. Top: Summer quality A, 81 cases. Middle: Winter quality A from tower 306, 83 cases. Winter quality A, other towers, 73 cases.
2.1.1 Signal duration

The duration of the recordings varied, and could last up to 15 seconds. The actual blast wave signals may have lasted up to a few seconds at long range, but often they were much shorter. Integrating over the whole recording could lead to overestimation of the SEL3 values because of noise. We therefore devised a very simple truncation algorithm: The timing \( t_p \) of peak pressure was identified, and then the surrounding time interval \( t_p - a < t < t_p + b \) was selected. For the summer quality A data, we set \( a = 0.5 \) s and \( b = 2 \) s. The resulting SEL3 spectra were practically identical to those using the whole recording. For the winter recordings, this was not the case, and we also changed the parameters to \( a = 1 \) s and \( b = 1.5 \) s, in order to accommodate some oddly shaped blast waves. These parameters were also used as control for the summer B1 data, and that gave small deviations from the untruncated recordings. Ideally, the B1 data should have been treated individually.

2.2 Weather data

The selected summer measurements are from six days in 1994. From September 13-14th, which seems to have featured cloudy weather and little temperature variation; and September 19-22nd, when the weather was clear with temperature inversions in the morning and large temperature variation throughout the day. An example of this weather type is shown in Figure 2.3. Winds were weak to moderate near ground, but ‘low level jets’ were observed at a few hundred meters height. These probably had significant impact on propagation, including during temperature inversions. The winter measurements were selected from February 21-23rd. The weather was then calm and clear with deep inversions, and large temperature variation throughout the day.

2.2.1 Tethersonde data interpretation

The tethersonde measured temperature, wind and wind direction at times \( t_k \) and heights \( z_k \) above ground. We used the Matlab interpolation routine ‘griddata’ to turn this into a map of the atmosphere across a continuum over \( t \) and \( z \). The result for one single day is shown in Figure 2.3. This interpolation routine responds strongly to how the parameters are scaled. We found through trial and error that dividing \( z \) with 5000 m/day gave reasonable looking results. Above the reach of the sonde we set wind and temperature constant.

For use in a propagation model, this two-dimensional map has to be reinterpreted into a four-dimensional map over time and space. The simplest strategy would be to follow the terrain, i.e. assume the meteorology is only a function of time and height above ground. A second strategy is to assume the meteorology is a function of time and altitude, i.e. height above sea level, only. This is likely a decent approximation except near the ground, and was our primary strategy. Exceptions were made for the following reason: The 403 station, where the sonde was operated, was at 320 m elevation, whereas station 306 was in a valley bottom at 280 m. As a solution, we let the weather follow the terrain whenever the ground elevation was below 320 m.

The tethersonde captured many details that were either intermittent fluctuations or just spurious artifacts. Neither are likely to be very useful for us, hence we applied some smoothing in the vertical
Figure 2.3  Top: Wind speed (m/s) as a function of time and height above ground on September 21st 1994. The tethersonde height is indicated by the black curve. Bottom: Temperature (°C) on September 21st.
direction to the data. The smoothing simply consisted of a running average. Unless otherwise noted, the temperature data were averaged over a 50 m window, and the wind data over 300 m. Another typical way to deal with this problem is to fit some function, such as a lin-log profile, to the data, but due to the large variety of observed profiles, smoothing seemed a better, less intrusive, option.

The summer tethersonde data were available in a postprocessed form in NORTRIAL, and we chose those. On September 21st there was a problem with the postprocessing, therefore the raw temperature data had to be used for that day. From the winter trials only unprocessed data were available. They were of course a bit noisier. The Matlab code we wrote to treat and interpolate the sonde data is included in appendix A.3 for completeness. There were many specific ‘glitches’ in the data that we corrected individually, and they are best listed in this way.

The lowest 10 m above ground, i.e. 320-330 m elevation, were not covered by the sonde data. We let the temperature be constant here, and let the wind taper off linearly to zero in the lowest 10 m above ground level. We also tested some surface layer models for the lowest few tens of meters above ground, and they are described later.

2.3 Ground data

It is crucial to have reasonably accurate values for the ground impedance $Z$. We calculated ground impedances from rigid porous medium models, based on parameters found in the database.

2.3.1 Summer

It is rather well-established that the Delany-Bazley model, although widely used in outdoor acoustics, is unsuitable for low frequencies, see e.g. [16] and [17]. We used a Taraldsen model ([17], [5]) instead. It requires one input parameter, the resistivity $\sigma$. The database provides a classification of the ground at Finnskogen, along with suggested values of $\sigma$, based on [14] and [15], see Figure 2.4. We used a halfspace model, as we had little information about vertical structure. Mostly the backing layer consisted of hard moraine. We suspect that deeper and more reflective layers played some role for infrasound at least at tower 112, based on looking at the spectra. At tower 306, sand sediments made up the backing layer. It has been demonstrated that this could lead to seismic effects ([10], [8]), which we have not attempted to include, partly because it may be difficult or impossible to model with an impedance boundary condition.

2.3.2 Winter

Snow 30-40 cm deep was reported from the winter trials, with significant terrain variability. Snow is expected to have a strong impact on sound levels in a way that is challenging to model. We tried to model the snow-covered ground as a rigid, homogeneous layer with a hard backing, as described in [5] and [12]. The Zwikker-Kosten model ([21], [12]) was chosen for the porous medium. This leaves three parameters to be chosen: resistivity $\sigma$, porosity $\Omega$, and snow depth $d$. Some clues to appropriate values were found in [13], however there seemed to have been a lack of data below
Figure 2.4  Ground classification. Values of specific resistivity $\sigma$ are given. Classes 0-1 are forest types, 2 marsh, 3 open country and 4 water.

40 Hz. We ended up with $\sigma = 8 \text{ kPa s/m}^2$, $\Omega = 0.7$ and $d = 70 \text{ cm}$. Obviously, the latter choice deviated from observed depths. On the other hand, the resulting impedance values captured the low frequency effects quite well, which was most important, since the main goal was to study the PE model and the weather data.

2.4 Source spectra

The source model is the so-called FOFT model described in [7]. The FOFT model is described for TNT, so we applied a conversion factor of 1.34 to the charge sizes. The model consists of a
Figure 2.6  Source spectra for 1 kg C4 for different ‘nonlinearity criteria’. The picture looks similar for other charges sizes.

blast wave from a free explosion evaluated at a range where the propagation is linear. The wave is then propagated backwards linearly to a reference length \( r_0 \). The range at which nonlinearities can be ignored is open for interpretation. We have chosen a peak pressure of 1 kPa as a criterion. The formulas indicate that it should rather be around 0.1 kPa, but at that range ground interaction and refraction are certainly more important. These two strategies differ by a few dB in the source spectra, as illustrated in Figure 2.6. Interesting experiments on ground interaction in the nonlinear range are reported in [3], where ground effects over grassland are observed already at 5 kPa.
3 Summer conditions study

We have gathered spectra for all 81 quality A summer cases in appendix A.2. The third octave SEL spectra from the PE simulations and the measurements can be compared for each case. For reference, we have included two simpler models: (1) PE simulations without refraction and topography, which resemble the Low Frequency Module currently implemented in Milnoise, and (2) a FOFT source model with a double charge. The double charge is a simple way to take the ground into account, because at close range most energy is reflected from the ground. Including this model in the plots demonstrates the effect of the propagation conditions. Next to each spectrum plot, the sound speed that was used in the simulation is shown as a function of altitude, with both the effective and the thermal sound speeds included.

3.1 All A data

Figure 3.1 shows the SELC values for all 81 cases. Predicted SELC is plotted against measured SELC. Hence, the prediction error can be read off as the vertical (or horizontal) distance to the black diagonal line. The PE predictions (blue circles) were scattered fairly symmetrically around the line, and the errors increased with decreasing SELC. The simple FOFT source model (light blue dots) overestimated SELC with minor exceptions, as should be expected over soft ground. The simple PE model (red dots) tended to underestimate. Both reference models deviated more for weak received signals.
Figure 3.2 shows the signed prediction errors in SELC plotted against range \( r \). The sign convention, which is used throughout this report, is such that positive values mean overprediction of sound levels. The errors were smallest at 1 km, and seem to increase until 6 km, beyond which there is no obvious pattern. It seems that the influence of the propagation conditions increased with range, as the three models increasingly deviated.

Figure 3.3 contains the error in SEL3 for all A data. The most striking feature is below 10 Hz, where the measurements at tower 306 consistently showed a strong sound reduction of up to tens of dB. As far as we know, there is no theoretical nor observed precedence for this phenomenon, hence it is best disregarded for now. The effect was evident also in [16], and, along with the above mentioned issues with tower 0, it can explain the difficulties reported there below 10 Hz. At tower 306, seismic effects have been predicted in the infrasound range, but the predicted magnitude was much smaller than the phenomenon observed here.

These experiments can not be regarded as statistically independent, and a statistical analysis is beyond the scope of this work. Certain features are clear, however, from the average quantities shown in Figures 3.4-3.5. Including weather improved both RMS (root mean square) error as well as median error, and increasingly so with frequency. The bias towards underestimation caused by ignoring weather is evident in the mean signed error. The variance of the error increased with frequency when weather was included. The lack of a strong bias in the predictions agrees with meteorological variability being the main source of uncertainty.

It is evident that weather and topography became more important as frequency and range increased. Hence, up to a certain range, a simpler algorithm such as the Milnoise LF module should suffice. Quantifying when and where is nontrivial, but the data may give us a clue. The band 1-25 Hz is regarded as particularly challenging, hence we consider the 25 Hz 3rd octave band. Figure 3.6 plots, against range, the differences in SEL3 between the full and the simple PE simulations. There are clear deviations at 2 km, and at 4 km, meteorology very obviously must be taken into account. At shorter ranges, ground interaction, or perhaps some other issue such as source modelling, are at least as critical as meteorology.
3.2 Weather types

The accuracy of sound propagation models should be expected to depend on the weather type. The accuracy of the weather forecast may vary with type, and the influence of atmospheric turbulence can be large when upward refraction or ground effect dominates.

As weather type indicators we chose the temperature gradient \( \tau = \Delta T / \Delta z \), evaluated as the change from 600 to 330 m altitude, and the wind component \( U \) in the direction of propagation at 600 m altitude. We also considered the effective sound speed gradient \( \Delta c_{\text{eff}} / \Delta z \), evaluated at the same heights as temperature. A scatter plot of the weather indicators for each case is provided in Figure 3.7. Cases with temperature inversion, i.e. with positive \( \tau \), were clearly separated, so we let them form one class. Downwind there will typically be some downward refraction, hence we divided the remaining cases at \( U = 2 \text{ m/s} \). The SEL3 errors are all plotted in Figure 3.8 with one colour for each weather type. The inversion cases were best captured, and the upwind/neutral cases the worst with a lot of underestimation. The latter was not unexpected.

Figure 3.9 shows the RMS errors for each weather class. It is evident that weather is crucial during inversion as well as downwind, while otherwise the weather data does not improve the RMS error much. Figure 3.11 shows SELC for each weather type. The SEL3 values at 32 Hz can be seen in Figure 3.10. The significance of weather is very clear at this frequency. The simple PE model underestimated during the downward refracting weather types. The full PE model clearly handled those weather types better, except for some long-range downwind cases, which were overestimated. The upwind/neutral situation is less clear: At longer range, the weather data enhanced underestimation, while at shorter range, they seem to have been quite useful. Generally, precision was much better for received SEL3 values above 80 dB than below.

SEL3 values for each of the three weather classes is provided as scatter plots in A.1-A.3 with one plot for each third octave band. The observations we have stated for 32 Hz hold generally. We
Figure 3.4  Top: Error in SEL3. Solid: RMS, dashed: median. Bottom: Mean signed error in SEL3. All summer A data.

Figure 3.5  Standard deviation from mean in SEL3 error. All summer A data.
Figure 3.6 Difference at 25 Hz in SEL3 between full and simple PE model. All summer A data.

Figure 3.7 Scatter plot of meteorological conditions. All summer A data. Circle sizes indicate range. Weather classifications marked with black lines.
Figure 3.8  RMS prediction error vs. f. Solid lines: Full PE, dashed: simple PE. Red: Inversion, green: downwind, blue: neither. Circle sizes are proportional to range. Summer A data.

Figure 3.9  RMS error for different weather types. Red: inversion, green: downwind, blue upwind/neutral. Solid lines are from the full PE simulations and dashed lines are from simple PE simulations. Summer A data.
also note a tendency towards over-prediction in the mid frequencies, perhaps to do with ground interaction or source modelling. At the lowest frequencies ground interaction and possibly other effects appear to have dominated over refraction in many cases.

### 3.3 Parameter variation

For this section, the numerical simulations of the summer quality A cases were repeated with various changes in the input data. This serves for one thing to illustrate some of the parametric uncertainty. A more ambitious aim is to determine which parameter choices are better.

#### 3.3.1 Topography

As mentioned, the terrain profiles were gentle by Norwegian standards. Topography had a direct effect, but it was relatively subtle. To illustrate this, we have performed the simulations without any refraction: Once with and once without topography. Figure 3.12 shows the difference in SEL3 due to including topography or not. Range and frequency played a role here as expected.

#### 3.3.2 Vertical regularisation

The vertical smoothing of temperature and wind is a balance act between capturing the essential features and excluding intermittent and/or spurious effects. As a less smoothed alternative we averaged temperature over 15 m and wind over 50 m. The scatter plots for each third octave are shown in Figure A.4-A.6. SEL3 values for 32 Hz are shown in Figure 3.13. We find that the increased detail tended to decrease accuracy, in some cases strongly so. In upwind conditions, detailed profiles may improve the underprediction problem, but at the price of occasional overestimates. Our findings are consistent with [20], in the sense that they recommend some averaging rather than instantaneous profiles. We have also tried to average temperature over 50 m as above and wind over 100 m, but it seems the rather large smoothing length of 300 m for the wind was favourable.
Figure 3.11  Predicted vs. measured SELC. Bottom: Neutral/upwind, middle: downwind, top: inversion. Summer A data.
Figure 3.12  Difference due to topography for 4 frequencies (denoted in Hz). No refraction. All summer A data.

Figure 3.13  Vertical smoothing of meteorology data at 32 Hz.
3.3.3 Surface layer

The surface layer (SL) is likely to be very complicated at a forest location like Finnskogen. We have still attempted some ways of taking it into account. Each attempt consisted of replacing the tethersonde data in the lowest few tens of meters above ground. We have tested the following ideas:

1. 'lin10'. No treatment (except for the usual linear tapering of the tethersonde wind data, hence the name).
2. 'log $z_0$'. Wind is replaced with a logarithmic profile

$$u(z) = u(z_t) \frac{\log(z/z_0 + 1)}{\log(z_t/z_0 + 1)}$$

with roughness length $z_0$ up to height $z_t$.
3. 'aws N'. A lin-log fit to the data from a weather tower at position N. Wind below 30 m above ground was then tapered to zero with the lin-log profile, keeping wind direction fixed. The temperature below 30 m was changed so that the gradient equaled that of the lin-log profile.

The simulation output was quite sensitive to the surface layer model, particularly for the higher frequencies. The scatter plots in Figure A.13 demonstrate this. None of the attempts seemed to improve on the simple 'lin10' model. The weather tower-based surface layer profiles notably increased the errors, which again shows that instantaneous, local profiles must be used with care.

Figure 3.14 compares the RMS error at short range for each SL model. Only the short range cases were included as they presumably are the most affected by the lowest parts of the atmosphere.

Looking at the weather tower data makes it clear that the SL profiles will vary a lot across the terrain. Figure 3.15 compares the temperature gradient between 10 and 30 meters at three locations over time. Most likely the profile depends a lot on local vegetation, and may behave somewhat stochastically. The wind profiles appeared more predictable, as they fit logarithmic profiles. At tower 0, a suitable roughness length seemed to be 10 m, while at 112, 2 m fit better. The ground class data explain the difference as 112 was in a field, and 0 was in open forest. The weather tower at 403 was inside dense and tall forest, and measured rather interesting profiles, as noted in [4].
3.3.4 Sound speed following topography

An alternative extrapolation of the sonde data is to assume that the meteorology only depends on height above ground. We show scatter plots from such a simulation in Figure A.7. At 306 we had to follow the terrain in any case, as already explained, therefore we only include data from tower 112 here. Results are not bad, but this alternative approach seems not to be very useful.

3.3.5 Scattering threshold

As mentioned, our scattering threshold was at -35 dB. Clearly, the sound levels still fall below the measured values in some cases. Figure 3.16 shows the RMS error in SEL3 resulting from different threshold values. For this statistic, the best choice was about -25 dB. Most likely, this should depend on the propagation conditions.

3.4 B1 data

The selection of quality B1 data was also simulated. The resulting SELC values look much as expected, see Figure 3.17. We divided weather types into downward and upward refracting according to the sign of the effective sound speed gradient. Ranges were either quite close at 2-4 km or above 10 km. The close range values were mostly well predicted, and the tether sonde data seem useful except for the underestimation at long range during upward refraction.
Figure 3.16  RMS for different scattering thresholds. The thresholds in dB are given.

Figure 3.17  Selected B1 data. Top: downward refraction. Bottom: upward refraction.
4 Winter conditions study

The spectra for the winter cases are included in appendix A.2. We first discuss the recordings from tower 306. Spectra for the cases with range 2 km are shown in Figure 4.1. These cases were used as templates to find suitable impedance values. It is clear that the ground effect was remarkably strong with a cut-off between 10 and 20 Hz. The cut-off was reasonably well captured by the simulations. Above 20 Hz sound levels varied a lot with weather, which makes it harder to assess the accuracy of the ground model.

All predicted SELC values are shown in Figure 4.2. There are large deviations compared to the summer cases. Without weather there was, as during summer, a bias towards underestimation. The SEL3 errors for all cases are plotted in 4.3. Accuracy decreased with frequency. We note that the unexplained damping of sound levels below 10 Hz is not present in the winter data.

The statistics in 4.4 look quite similar to the summer data, but RMS errors and biases are both larger. It is still clear though, that the tethersonde data improved predictions.

Temperature inversions were deeper in winter, hence weather type indicators are evaluated higher up: The temperature gradient \( \tau = \Delta T / \Delta z \) is the change from 820 to 350 m altitude. The same applies for \( c_{\text{eff}} \) gradient. The wind indicator \( U \) is evaluated at 710 m altitude. Weather type indicators are plotted in Figures 4.5-4.6. For classification of weather types we simply divide into upward and downward refraction according to the sign of the \( c_{\text{eff}} \) gradient. SELC errors are plotted against the \( c_{\text{eff}} \) gradient in Figure 4.7. The RMS errors did not vary much between these two weather classes, except that they were large for the simple PE model during downward refraction.

It is clear that the winter data are very challenging to model. This is, at least partly, due to the snow cover. It may be that the strong ground damping made scattering effects more prominent. Other possible explanations are that the postprocessing had been applied to the summer tethersonde data and not the winter data, and that therefore there are more spurious features in the winter sound speed profiles. Also, it may be that the weather conditions happened to be more challenging during the winter trials. There was a larger proportion of long ranges in the winter data, which explains some, but not all of the increased difficulty.

4.1 Parameter studies

A few variations of the simulation setup was attempted for the winter trials.

4.1.1 Ground impedance

Two ground impedance strategies are compared in Figure A.12. Different snow depths are supplied to the hard-backed Zwikker-Kosten model. Other parameters remain constant. The 35 cm choice yields too large sound levels for the lower frequencies, but otherwise the results are practically identical.
Figure 4.1  Range 2 km at tower 306. 1 kg charges. Microphone heights vary. Blue lines are measurements and black lines are simple PE simulations.

Figure 4.2  All cases.

Figure 4.3  Errors in SEL3 for all winter cases at tower 306.
Figure 4.4 Mean quantities for the winter A cases from tower 306. Dashed lines are median errors, solid lines are RMS errors.
Figure 4.5  Sound speed gradient vs. temperature gradient. Winter. Circle size is proportional to range.

Figure 4.6  Wind vs. temperature gradient. Winter. Circle size is proportional to range.

Figure 4.7  SELC error vs. effective sound speed gradient. Winter. Circle size is proportional to range.
4.1.2 Surface layer

The simple 'lin10' model seems to outperform the logarithmic SL wind profile, see Figure A.13 in the Appendix.

4.1.3 Vertical regularisation

We tried out doubling the vertical smoothing lengths. Resulting SEL3 values at 64 Hz are shown in Figure 4.8. The data are plotted against effective sound speed gradient. It seems that more smoothing might be beneficial near neutral conditions, i.e. when the sound speed gradient is small. For downward refraction, too much smoothing reduces precision. We remark that the logarithmic surface layer tapering of wind was used for all simulations shown in 4.8. The plots of the sound speed in appendix A.2 suggest that the unprocessed temperature data could be less reliable than unprocessed summer data. Hence we tried an experiment with a 300 m smoothing window in both temperature and wind speed. Results were markedly different, but none consistently better than the other.

4.2 Data from towers 212 and 412

The remaining cases of quality A were from towers 212 and 412. As mentioned, the charge sizes had to be retrieved from tower 306 data entries, hence we regard these data with enough suspicion to treat them separately. SELC values are shown in Figure 4.9. There were 59 long distance cases with range exceeding 10 km, and the remaining 15 were at 4 km or less. The third octave scatter plots can be seen in Figures A.14-A.15.

We note that four of the downward refraction cases are badly underestimated. These were at ranges 22-23 km from around the same time. At this range one should expect that the tethersonde data are insufficient, because there may be important downward refracting conditions higher up in
the atmosphere, and also because the horizontal homogeneity assumption is less likely to be valid. There are nine upward refracting cases that are badly underestimated. These are all from the same 14 km path (108->412) and around the same time, indicating that there is a weather feature that is not captured properly. We note also a tendency towards overestimation of the stronger signals. We believe this is due to ground interaction, because of deeper, or a different type of, snow around these receiver locations. Indeed, we observe that the cut-off frequency is lower at tower 412 than at 306, when examining the spectra for the close range cases.
5 Summary

We make the following conclusions from this validation study:

1. The PE model worked as well as can be expected given the parametric uncertainties.
2. Taking the weather into account is clearly necessary in noise mapping of heavy weapons and explosions.
3. The tethersonde weather data improved predictions.
4. Model performance in summer was good during downward refracting conditions, and less so during upward refraction. Difficulty with upward refraction is commonly observed in outdoor acoustics, and believed to be due to scattering from turbulence.
5. The PE model with tethersonde data gave on average very good predictions, in the sense that there was little modelling bias. There was one exception: At long range during upward refraction, we observed strong underestimation. During downward refraction, there was on average a few dB overestimation.
6. Ground interaction in winter was very strong and difficult to model.
7. Winter data were not as accurately predicted as summer data, at least partly due to the ground interaction. Tethersonde data were still helpful.
8. The importance of weather increased with frequency and range.
9. Louder sounds were more accurately predicted than softer sounds. This has to do with both range and refractive conditions.
10. The ground impedance data for summer conditions seemed to be fairly accurate.
11. Infrasound prediction required weather data from 2-4 km range. At closer range other effects were equally or more important.
12. The level of detail to take into account from localised weather profiles needs to strike a balance between capturing essential features and avoiding small scale fluctuations.
13. Surface layer modelling influenced the simulation results. Simple SL models were better than using instantaneous profiles from weather towers.

Generalisation of these conclusions may be limited to the weather types tested; in particular, strong winds did not occur during the experiments. Also, it should be noted that actual training activity often takes place in somewhat more rugged terrain than at Finnskogen.

The main goal, to validate the PE model, has been addressed, and we have obtained additional valuable insights. Even so, this study leaves many questions unanswered that could be addressed by further investigation:

1. Could more simple weather profiles be useful? It would be interesting, from a practical viewpoint, to look at sound speed profiles based on reduced data, perhaps even purely based on ground measurements.
2. How important is turbulent scattering? It is likely to be important due to the underestimated long range upwind cases, although this could also occur due to the large scale sound speed profiles being incorrect. A correlation study of closely timed detonations would clarify this.
3. What is the best way of modelling these scattering effects? This is an on-going research field in outdoor acoustics. Current methods are computationally expensive, and have limited
applicability to complicated long-range scenarios. Hence, this is a rather challenging question. Perhaps some empirically based statistical strategy should be sought, such as in [9].

4. How can the surface layer best be handled? This question is closely connected to the previous one.

5. Can the ground impedance values be improved? For summer, this might be possible from looking at short range cases.

6. How should ground impedance be computed over snow? This is certainly worth more attention, although it seems to be a very challenging topic.

7. Why are the winter data less accurately predicted than the summer data? Extreme, possibly inaccurate, impedance values in combination with scattering effects seem very likely reasons. It could also be related to the weather data, but that is difficult to judge without understanding the ground interaction.

8. The treatment of the nonlinear propagation near the source leaves a few dB of uncertainty. In practice, this may be hard to tease out from the uncertainty in ground impedance, and may be site specific. The shorter range NORTRIAL measurements from Haslemoen are more suited for this.

9. Vegetation and topographic roughness were not taken into account here, except perhaps indirectly via the impedance boundary. This is a tricky issue in itself, and especially when there are so many other unknown factors.

10. How good is the assumption of horizontal homogeneity of atmospheric conditions? At times at least, it is remarkably good, as shown in [4]. A more systematic study would be useful.

11. Comparison with other propagation models, such as ray-tracing, Fast Field Program and engineering standards may be interesting. These methods lack generality, but, when applicable, are more efficient than PE methods.
A Appendix

A.1 Scatter plots

Third octave sound exposure levels, SEL3, are presented here as scatter plots with measurements along the x-axis and predictions along the y-axis. The diagonal is drawn as a solid line, and the center frequency is indicated above each plot.

Figure A.1 Predicted vs. measured 3rd octave SEL during temperature inversion, summer A data, 27 cases.
Figure A.2  Predicted vs. measured 3rd octave SEL downwind, summer A, 19 cases.
Figure A.3  Predicted vs. measured 3rd octave SEL upwind or neutral, summer A, 34 cases.
Figure A.4  Smoothing study, summer A, temperature inversion.
Figure A.5  Smoothing study, summer A, downwind.
Figure A.6  Smoothing study, summer A, upwind/neutral.
Figure A.7  Terrain-following sonde data. Summer A, tower 112, 18 cases.
Figure A.8  Logarithmic surface layer profiles. Summer A. Range less than 2.1 km, 29 cases.
Figure A.9  Weather tower data as SL models. Range less than 2.1 km, 29 cases.
Figure A.10  Downward refraction, winter A, tower 306, 49 cases
Figure A.11  Upward refraction, winter A, tower 306, 34 cases
Figure A.12  Winter A, tower 306, 83 cases. Snow depth in impedance model varied.
Figure A.13  Winter A, tower 306, 2 km range, 20 cases. Surface layer models.
Figure A.14 Winter A, towers 212 and 412. Downward refraction, 45 cases.
Figure A.15  Winter A, towers 212 and 412. Upward refraction, 29 cases.
A.2

For each plot the following information is listed: A case number assigned by us, the event number of the detonation, the source and receiver, locations, the charge size, the receiver heights, the date and time. Spectra across 4-100 Hz are plotted with a logarithmic $f$-axis. The red solid lines are measured spectra. Blue simulated, dashed black the simple PE results, and blue circles the source model. Horizontal black lines in the sound speed plots indicate the minimum of source and receiver elevation. The sound speed profiles used in m/s are plotted against altitude: effective sound speed in blue and thermal sound speed in red.
A.2.1 Summer A data

Figure A.16
Figure A.17
Figure A.18
Figure A.19
Figure A.21
A.2.2 Winter A data

The first 83 are the ones from tower 306.
Figure A.23
Figure A.24
Figure A.25
Figure A.27
Figure A.28
Figure A.29
Figure A.30
Figure A.31
Figure A.33
Figure A.34
Figure A.35
Figure A.36
A.3 Tethersonde data processing

Summer data:

```matlab
% Read tethersonde data
[z3, ws3, wd3, at3raw, ap3, t3raw] = gettethparams_mod_kw(403, 1994, metbase94); % Raw T-data

[t3, ws3, wd3, at3, ap3, t3] = gettethparams(403, 1994, metbase94);

tsep01_94 = date2num('01-Sep-1994', '00:00:00.000');
tstart = tsep01_94 - 1;

% Remove bad data (usually when sonde just had a break)
jT = find(t3raw - tstart < 21.289 & t3raw - tstart > 21.28); % Botched T-data
at3raw(jT) = at3raw(jT(end));
jT = find(t3 - tstart < 21.289 & t3 - tstart > 21.28); % Botched T-data
at3(jT) = at3(jT(end));
wd3(jT) = wd3(jT(end));
ws3(jT) = ws3(jT(end));
z3(jT) = z3(jT(end));
jT = find(t3 - tstart < 22.3 & t3 - tstart > 22.2); % Botched T-data
at3(jT) = interp1(t3([jT(1), jT(end)]), at3([jT(1), jT(end)]), t3(jT));
wd3(jT) = interp1(t3([jT(1), jT(end)]), wd3([jT(1), jT(end)]), t3(jT));
ws3(jT) = interp1(t3([jT(1), jT(end)]), ws3([jT(1), jT(end)]), t3(jT));

% Remove bad data (usually when sonde just had a break)
jT = find(t3 - tstart < 13.564 & t3 - tstart > 13.559); % Botched T-data
at3(jT) = interp1(t3([jT(1), jT(end)]), at3([jT(1), jT(end)]), t3(jT));
wd3(jT) = interp1(t3([jT(1), jT(end)]), wd3([jT(1), jT(end)]), t3(jT));
ws3(jT) = interp1(t3([jT(1), jT(end)]), ws3([jT(1), jT(end)]), t3(jT));

% Remove bad data (usually when sonde just had a break)
jT = find(t3 - tstart < 13.65 & t3 - tstart > 13.63); % Botched T-data
at3(jT) = at3(jT(1));
wd3(jT) = wd3(jT(1));
ws3(jT) = ws3(jT(1));

% Remove bad data (usually when sonde just had a break)
jT = find(t3 - tstart < 14.352 & t3 - tstart > 14.33); % Botched T-data
at3(jT) = at3(jT(end));
wd3(jT) = wd3(jT(end));
ws3(jT) = ws3(jT(end));

% Remove bad data (usually when sonde just had a break)
jT = find(t3 - tstart < 19.362 & t3 - tstart > 19.31); % Botched T-data
at3(jT) = at3(jT(end));
wd3(jT) = wd3(jT(end));
ws3(jT) = ws3(jT(end));
```
\[ jT = \text{find} (t3 - t_{\text{start}} < 20.303 \& t3 - t_{\text{start}} > 20.3) ; \% \text{Botched T-data} \]

\[ at3(jT) = at3(jT_{\text{end}}); \]

\[ wd3(jT) = wd3(jT_{\text{end}}); \]

\[ ws3(jT) = ws3(jT_{\text{end}}); \]

\[ jT = \text{find} (t3 - t_{\text{start}} < 20.48 \& t3 - t_{\text{start}} > 20.405); \% \text{Botched T-data} \]

\[ at3(jT) = at3(jT_{1}); \]

\[ wd3(jT) = wd3(jT_{1}); \]

\[ ws3(jT) = ws3(jT_{1}); \]

\[ jT = \text{find} (t3 - t_{\text{start}} < 20.524 \& t3 - t_{\text{start}} > 20.5); \% \text{Botched T-data} \]

\[ at3(jT) = at3(jT_{1}); \]

\[ wd3(jT) = wd3(jT_{1}); \]

\[ ws3(jT) = ws3(jT_{1}); \]

\[ jT = \text{find} (\text{not} (t3 - t_{\text{start}} < 22.303 \& t3 - t_{\text{start}} > 22.1)); \% \text{Botched T-data (remove)} \]

\[ z3 = z3(jT); \]

\[ t3 = t3(jT); \]

\[ at3 = at3(jT); \]

\[ wd3 = wd3(jT); \]

\[ ws3 = ws3(jT); \]

\[ jT = \text{find} (\text{not} (t3 - t_{\text{start}} < 14.7 \& t3 - t_{\text{start}} > 14.623)); \% \text{Botched T-data (remove)} \]

\[ z3 = z3(jT); \]

\[ t3 = t3(jT); \]

\[ at3 = at3(jT); \]

\[ wd3 = wd3(jT); \]

\[ ws3 = ws3(jT); \]

\[ jT = \text{find} (\text{not} (t3 - t_{\text{start}} < 23 \& t3 - t_{\text{start}} > 22.530)); \% \text{Botched T-data (remove)} \]

\[ z3 = z3(jT); \]

\[ t3 = t3(jT); \]

\[ at3 = at3(jT); \]

\[ wd3 = wd3(jT); \]

\[ ws3 = ws3(jT); \]

\[ \cos EW3 = \cos((90 - wd3) * \pi / 180); \]

\[ \cos NS3 = \cos(wd3 * \pi / 180); \]

\[ uwe = ws3. * (-\cos EW3); \]

\[ usn = ws3. * (-\cos NS3); \]

\[ \% \text{Replace 21/9 with raw data.} \]

\[ tsep = t3 - t_{\text{start}}; \]

\[ jT = \text{find} (\text{abs}(tsep - 21.5) < .5); \]

\[ tsepraw = t3raw - t_{\text{start}}; \]

\[ jtraw = \text{find} (\text{abs}(tsepraw - 21.5) < .5); \]

\[ at3(jT) = at3raw(jtraw); \]
% Interpolation to cartesian grid
[tt, zz] = meshgrid(13:.02:23, 10:5:1010);
TT = griddata(t3-tstart, z3/5000, at3, tt, zz/5000); % Note scaling of z
uu = griddata(t3-tstart, z3/5000, uwe, tt, zz/5000);
vv = griddata(t3-tstart, z3/5000, usn, tt, zz/5000);

% Above the grid etc:
[nz nt] = size(tt);
maxh = tethpeak_kw(z3, 200); % Upper height of each tethersonde flight
ttops = t3(maxh(:, 2)) - tstart;
ztops = maxh(:, 1);
t = tt(1, :);
zcut = interp1(ttops, ztops, t, 'linear', 'extrap');

for jt = 1: nt % Loop over times in interp grid
    iinan = find(isnan(TT(:, jt)) | zz(:, jt) > zcut(jt));
    iinan = min(iinan);
    iinan = max(2, iinan);
    TT(iinan:end, jt) = TT(iinan - 1, jt);
    iinan = find(isnan(uu(:, jt)) | zz(:, jt) > zcut(jt));
    iinan = min(iinan);
    iinan = max(2, iinan);
    uu(iinan:end, jt) = uu(iinan - 1, jt);
    iinan = find(isnan(vv(:, jt)) | zz(:, jt) > zcut(jt));
    iinan = min(iinan);
    iinan = max(2, iinan);
    vv(iinan:end, jt) = vv(iinan - 1, jt);
end

% Outside data, set to 0:
TT(isnan(TT)) = 0;
uu(isnan(uu)) = 0;
vv(isnan(vv)) = 0;

% Save to file readable by write_weatherfile.m
save tethdatainterp2 tt zz uu vv TT t zcut

Winter data:
[z3, ws3, wd3, at3, ap3, t3] = gettethparams(403, 1996, metbase96);
wdl = wd1 - 180;
h3 = 320 + z3;
tfeb01_96 = date2num( '01-Feb-1996' , '00:00:00.000' );
tstart = tfeb01_96 - 1;

jyes3 = find ( z3 > 0);
  z3 = z3 ( jyes3 );
  ws3 = ws3 ( jyes3 );
  wd3 = wd3 ( jyes3 );
  at3 = at3 ( jyes3 );
  t3 = t3 ( jyes3 );

jyes3 = find ( z3 < 1050);
  z3 = z3 ( jyes3 );
  ws3 = ws3 ( jyes3 );
  wd3 = wd3 ( jyes3 );
  at3 = at3 ( jyes3 );
  t3 = t3 ( jyes3 );

jyes3 = find ( at3 < -2.5);
  z3 = z3 ( jyes3 );
  ws3 = ws3 ( jyes3 );
  wd3 = wd3 ( jyes3 );
  at3 = at3 ( jyes3 );
  t3 = t3 ( jyes3 );

whichdate = floor ( t3 - tstart );
  jyes3 = find ( whichdate == 22 | ( at3 < -8 & whichdate == 22 ) );
  z3 = z3 ( jyes3 );
  ws3 = ws3 ( jyes3 );
  wd3 = wd3 ( jyes3 );
  at3 = at3 ( jyes3 );
  t3 = t3 ( jyes3 );

whichdate = floor ( t3 - tstart );
  jyes3 = find ( whichdate == 21 | ( at3 > -11 & whichdate == 21 ) );
  z3 = z3 ( jyes3 );
  ws3 = ws3 ( jyes3 );
  wd3 = wd3 ( jyes3 );
  at3 = at3 ( jyes3 );
  t3 = t3 ( jyes3 );

jyes3 = find ( t3 - tstart > 21.531);
  z3 = z3 ( jyes3 );
  ws3 = ws3 ( jyes3 );
  wd3 = wd3 ( jyes3 );
  at3 = at3 ( jyes3 );
  t3 = t3 ( jyes3 );

jyes3 = find ( t3 - tstart < 21.6505 | t3 - tstart > 21.652);
  z3 = z3 ( jyes3 );
  ws3 = ws3 ( jyes3 );
  wd3 = wd3 ( jyes3 );
  at3 = at3 ( jyes3 );
  t3 = t3 ( jyes3 );

jyes3 = find ( t3 - tstart > 22.345 | t3 - tstart < 22.3);
  z3 = z3 ( jyes3 );
  ws3 = ws3 ( jyes3 );
  wd3 = wd3 ( jyes3 );
  at3 = at3 ( jyes3 );
  t3 = t3 ( jyes3 );

jyes3 = find ( t3 - tstart < 21.6505 | t3 - tstart > 21.653);
  z3 = z3 ( jyes3 );
  ws3 = ws3 ( jyes3 );
  wd3 = wd3 ( jyes3 );
  at3 = at3 ( jyes3 );
  t3 = t3 ( jyes3 );

jyes3 = find ( t3 - tstart < 22.385 | t3 - tstart > 22.3856);
  z3 = z3 ( jyes3 );
  ws3 = ws3 ( jyes3 );
  wd3 = wd3 ( jyes3 );
  at3 = at3 ( jyes3 );
  t3 = t3 ( jyes3 );

jyes3 = find ( t3 - tstart < 21.613 | t3 - tstart > 21.615);
  z3 = z3 ( jyes3 );
  ws3 = ws3 ( jyes3 );
  wd3 = wd3 ( jyes3 );
  at3 = at3 ( jyes3 );
  t3 = t3 ( jyes3 );

jyes3 = find ( t3 - tstart < 22.436 | t3 - tstart > 22.489);
  z3 = z3 ( jyes3 );
  ws3 = ws3 ( jyes3 );
  wd3 = wd3 ( jyes3 );
  at3 = at3 ( jyes3 );
  t3 = t3 ( jyes3 );
jyes3 = find(t3 - tstart < 23.374 | t3 - tstart > 23.377);
jyes3 = find(t3 - tstart < 23.438 | t3 - tstart > 23.445);
jyes3 = find(ws3 > 0 & ws3 < 8);
jyes3 = find(t3 - tstart < 22.48 | t3 - tstart > 22.51);

% \texttt{uEW} = ws3 \cdot \cos WE3;

\begin{verbatim}
\texttt{c_of_T = @(T) 20.03 \times \sqrt{T+273.15};}\%linear: \texttt{cst = 340 + 0.6*(T-15);} \texttt{cosEW3 = cos((90-wd3)*\pi/180);} \texttt{cosNS3 = cos(wd3*\pi/180);} \texttt{uwe = ws3.*(-cosEW3);} \texttt{usn = ws3.*(-cosNS3);} \texttt{\%Interpolation of the thersonde data} \texttt{[tt, zz] = meshgrid(21:0.002:29,0:5:1010);} \texttt{TT = griddata(t3 - tstart, z3/5000, at3, tt, zz/5000);} \%Note scaling of z \texttt{uu = griddata(t3 - tstart, z3/5000, uwe, tt, zz/5000);} \texttt{vv = griddata(t3 - tstart, z3/5000, usn, tt, zz/5000);} \texttt{\%Above the grid etc:} \texttt{[nz, nt] = size(tt);} \texttt{maxh = tethpeak_kw(z3,800);} \texttt{\%Upper height of each thersonde flight} \texttt{ttops = t3(maxh(:,2)) - tstart;} \texttt{ztops = maxh(:,1);} \texttt{t = tt(1,:);} \texttt{zcut = interp1(ttops, ztops, t, 'linear', 'extrap');} \texttt{for jt = 1:nt \% Loop over times in interp grid} \texttt{ iinan = find(zz(:,jt) > zcut(jt));} \texttt{ iinan = min(iinan);} \texttt{ iinan = max(2, iinan);} \texttt{ TT(iinan:end, jt) = TT(iinan-1, jt);} \texttt{ iinan = find(zz(:,jt) > zcut(jt));} \texttt{ iinan = min(iinan);} 
\end{verbatim}

\begin{verbatim}
iinan = max(2, iinan);
uu(iinan:end, jt) = uu(iinan-1, jt);
iinan = find(zz(:,jt)>zcut(jt));
iinan = min(iinan);
iinan = max(2, iinan);
vv(iinan:end, jt) = vv(iinan-1, jt);
end

% Outside data, set to 0:
TT(isnan(TT)) = griddata(t3-tstart, z3/5e3, at3-tt(isnan(TT)), zz(isnan(TT))/5e3, 'nearest');
uu(isnan(uu)) = griddata(t3-tstart, z3/5e3, uwe, tt(isnan(uu)), zz(isnan(uu))/5e3, 'nearest');
vv(isnan(vv)) = griddata(t3-tstart, z3/5e3, usn, tt(isnan(vv)), zz(isnan(vv))/5e3, 'nearest');

% Save to file readable by write_weatherfile.m
save tethdatainterpF96 tt zz uu vv TT
\end{verbatim}

A.4 Lists of NORTRIAL data selections

This section lists the selected data from the NORTRIAL database. We provide a case number (case, defined in this report), a detonation event number (event, defined in NORTRIAL), the receiver position (rec), and receiver height in m (h(m)). The latter three pieces of information uniquely define the recording. We also list the measured (SELCnt) and simulated (SELCpe) C-weighted SEL values.

A.4.1 Summer quality A data

\begin{center}
\begin{tabular}{cccccccc}
\hline
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Bibliography


About FFI
The Norwegian Defence Research Establishment (FFI) was founded 11th of April 1946. It is organised as an administrative agency subordinate to the Ministry of Defence.

FFI’s MISSION
FFI is the prime institution responsible for defence related research in Norway. Its principal mission is to carry out research and development to meet the requirements of the Armed Forces. FFI has the role of chief adviser to the political and military leadership. In particular, the institute shall focus on aspects of the development in science and technology that can influence our security policy or defence planning.

FFI’s VISION
FFI turns knowledge and ideas into an efficient defence.

FFI’s CHARACTERISTICS
Creative, daring, broad-minded and responsible.

Om FFI
Forsvarets forskningsinstitutt ble etablert 11. april 1946. Instituttet er organisert som et forvaltningsorgan med særlige fullmakter underlagt Forsvarsdepartementet.

FFIs FORMÅL

FFIs VISJON
FFI gjør kunnskap og ideer til et effektivt forsvar.

FFIs VERDIER
Skapende, drivende, videnskt og ansvarlig.

FFI’s organisation